

TOPIC : 8 ELECTRIC FLUX DENSITY GAUSS LAW & DIVERGENCE

1. Determine \vec{D} at $(4, 0, 3)$ if there is a point charge $-5\pi(\text{mc})$ at $(3, 0, 0)$ and a line charge $37\pi(\text{mc})$ along y axis.
2. A charge configuration is given by $\rho_v = 5\rho e^{-2\rho} \text{ C/m}^3$. Find \vec{D} using Gauss's law.
3. Find the flux density at a point A $(6, 4, -3)$ caused by:
(a) a point charge of 20mc at the origin.
(b) a uniform line charge $\rho_L = 20\text{nC/m}$ on the z axis.
(c) a uniform sheet charge density $\rho_s = 60\text{nC/m}^2$ at a plane $x = 8$.
4. State and explain Gauss's law with its mathematical proof.
5. Explain Gauss' law applied to differential volume element.
6. Explain Divergence's Theorem.
7. Find divergence D at the origin if
$$D = e^{-x} \cdot \sin y \vec{a}_x - e^{-x} \cdot \cos y \vec{a}_y + 2z \vec{a}_z$$
8. Let $D = 2xy^2z^3 \vec{a}_x + 3xy^3z^3 \vec{a}_y + 2xyz^3 \vec{a}_z \text{ C/m}^2$ in free space. Find (a) The total electrical flux passing through the surface $x=2$, $0 \leq y \leq 2$, and $0 \leq z \leq 2$ in a direction away from the origin.
(b) The total charge contained in an incremental sphere of a radius 1 Nm centered at $P(9, 9, 9)$.